

-NoValue-

axd.1 Derivações with Quantifiers

fol:axd:prq:
sec

Exemplo axd.1. Let us give a **derivação** of $(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow \forall x (\varphi(x) \wedge \psi(x))$.

First, note that

$$(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow \forall x \varphi(x)$$

is an instance of ??, and

$$\forall x \varphi(x) \rightarrow \varphi(a)$$

of ??. So, by ??, we know that

$$(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow \varphi(a)$$

is **derivável**. Likewise, since

$$\begin{aligned} (\forall x \varphi(x) \wedge \forall y \psi(y)) &\rightarrow \forall y \psi(y) && \text{and} \\ &\forall y \psi(y) \rightarrow \psi(a) \end{aligned}$$

are instances of ?? and ??, respectively,

$$(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow \psi(a)$$

is derivable by ??. Using an appropriate instance of ?? and two applications of MP, we see that

$$(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow (\varphi(a) \wedge \psi(a))$$

is derivable. We can now apply QR to obtain

$$(\forall x \varphi(x) \wedge \forall y \psi(y)) \rightarrow \forall x (\varphi(x) \wedge \psi(x)).$$

Créditos das Imagens

Referências Bibliográficas