

-NoValue-

thy.1 Coding Computations

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sec In every model of computation, it is possible to do the following:

1. Describe the *definitions* of computable functions in a systematic way. For instance, you can think of Turing machine specifications, recursive definitions, or programs in a programming language as providing these definitions.
2. Describe the complete record of the computation of a function given by some definition for a given input. For instance, a Turing machine computation can be described by the sequence of configurations (state of the machine, contents of the tape) for each step of computation.
3. Test whether a putative record of a computation is in fact the record of how a computable function with a given definition would be computed for a given input (on which the function is defined, O.s., the computation halts).
4. Extract from such a description of the complete record of a computation the value of the function for a given input. For instance, the contents of the tape in the very last step of a halting Turing machine computation is the value.

Using coding, it is possible to assign to each description of a computable function a numerical *index* in such a way that the instructions can be recovered from the index in a computable way. Similarly, the complete record of a computation can be coded by a single number as well. The resulting arithmetical relation “*s* codes the record of computation of the function with index *e* for input *x*” and the function “output of computation sequence with code *s*” are then computable; in fact, they are primitive recursive.

This fundamental fact is very powerful, and allows us to prove a number of striking and important results about computability, independently of the model of computation chosen.

Créditos das Imagens

Referências Bibliográficas